

1. The length of the diagonal of square S , as well as the lengths of the diagonals of rhombus R are integers. The ratio of the lengths of the diagonals is $15:11:9$, respectively. Which of the following could be the difference between the area of square S and the area of rhombus R ?

- I. 63
- II. 126
- III. 252

- A. I only
- B. II only
- C. III only
- D. I and III only
- E. I, II and III

2. Set S contains 7 different letters. How many subsets of set S , including an empty set, contain at most 3 letters?

- A. 29
- B. 56
- C. 57
- D. 63
- E. 64

3. How many different subsets of the set $\{0, 1, 2, 3, 4, 5\}$ do not contain 0?

- A. 16
- B. 27
- C. 31
- D. 32
- E. 64

4. The functions f and g are defined for all the positive integers n by the following rule: $f(n)$ is the number of perfect squares less than n and $g(n)$ is the number of primes numbers less than n . If $f(x) + g(x) = 16$, then x is in the range:

- A. $30 < x < 36$
- B. $30 < x < 37$
- C. $31 < x < 37$
- D. $31 < x < 38$
- E. $32 < x < 38$

5. Which of the following is a factor of $18!+1$?

- A. 15
- B. 17
- C. 19
- D. 33
- E. 39

6. If the least common multiple of a positive integer x , 4^3 and 6^5 is 6^6 . Then x can take how many values?

- A. 1
- B. 6
- C. 7
- D. 30
- E. 36

7. The greatest common divisor of two positive integers is 25. If the sum of the integers is 350, then how many such pairs are possible?

- A. 1
- B. 2
- C. 3
- D. 4
- E. 5

8. The product of a positive integer x and 377,910 is divisible by 3,300, then the least value of x is:

- A. 10
- B. 11
- C. 55
- D. 110
- E. 330

9. What is the 101st digit after the decimal point in the decimal representation of $\frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \frac{1}{37}$?

- A. 0
- B. 1
- C. 5
- D. 7
- E. 8

10. If x is not equal to 0 and $x^y = 1$, then which of the following must be true?

- I. $x = 1$
- II. $x = 1$ and $y = 0$
- III. $x = 1$ or $y = 0$

- A. I only
- B. II only
- C. III only
- D. I and III only
- E. None